

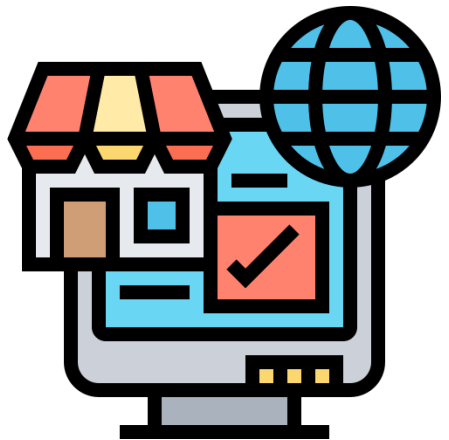
Fast and Multi-aspect Mining of Complex Time-stamped Event Streams

Kota Nakamura, Yasuko Matsubara, Koki Kawabata,
Yuhei Umeda, Yuichiro Wada, Yasushi Sakurai



Complex Time-stamped Event Streams are Everywhere

- A huge, online stream of time-stamped events with multiple attributes



E-commerce



Local mobility

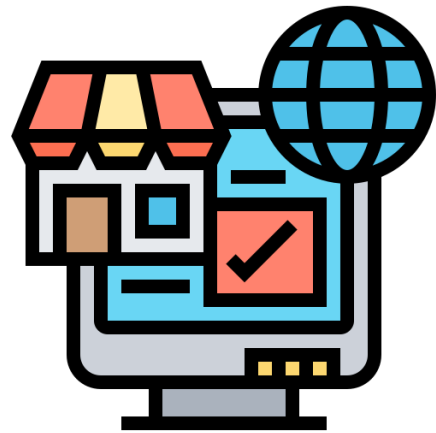


CyberSecurity

Complex Time-stamped Event Streams are Everywhere

- A huge, online stream of time-stamped events with multiple attributes

3 attributes (M=3)



E-commerce

TimeStamp	Brand	Item category	Price
2023-04-30-21:01	Tefal	Kettle	\$45
2023-04-30-21:01	Bosch	Refrigerator	\$200
2023-04-30-21:02	Samsung	TV	\$650
2023-04-30-21:03	Sony	Portable audio	\$200
2023-04-30-21:08	LG	TV	\$400
2023-04-30-21:11	Dell	Monitor	\$90
2023-04-30-21:13	Philips	Headphones	\$190

Complex Time-stamped Event Streams are Everywhere

- A huge, online stream of time-stamped events with multiple attributes

2 attributes ($M=2$)



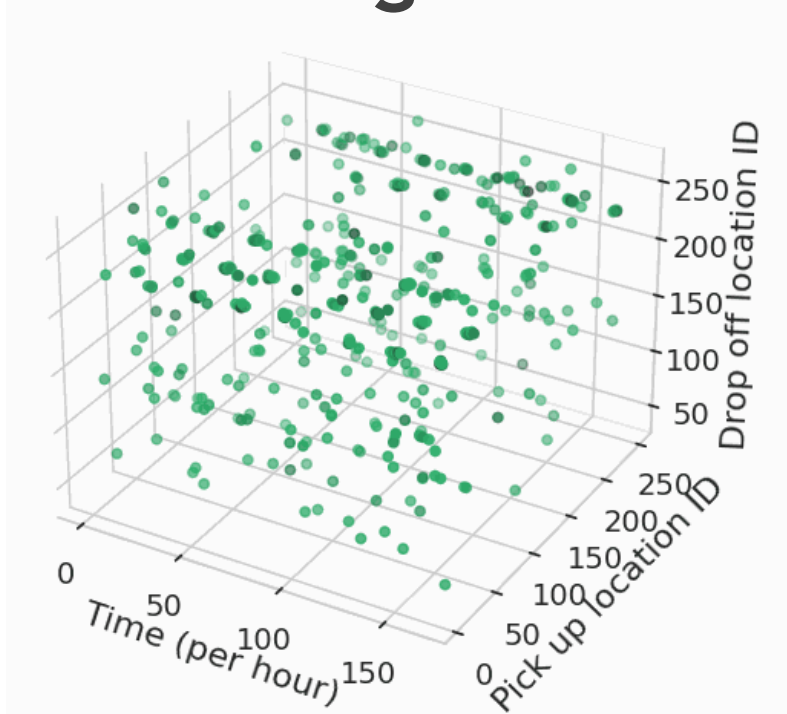
Local mobility

TimeStamp	Pick-up location	drop-up location
2023-04-30-20:01	Museum C	Museum B
2023-04-30-21:02	Cinema A	Street C
2023-04-30-21:06	School D	Restaurant A
2023-04-30-21:18	Office A	Station A
2023-04-30-22:08	Street A	University D
2023-05-01-09:11	Hotel B	Airport A
2023-05-01-11:13	Station C	Street B

Limitations & Challenges

Complex time-stamped event streams ...

derail existing methods and even our interpretation



3rd -order tensor stream:
each aspect indicates each attributes

Because this is...

High-order tensor streams

 **High-dimensional**

 **Sparse**

 **Semi-infinite**

Our Questions

- Q. How can we **summarize** large, dynamic high-order tensor streams?
- Q. How can we see any hidden **patterns**, **rules**, and **anomalies**?

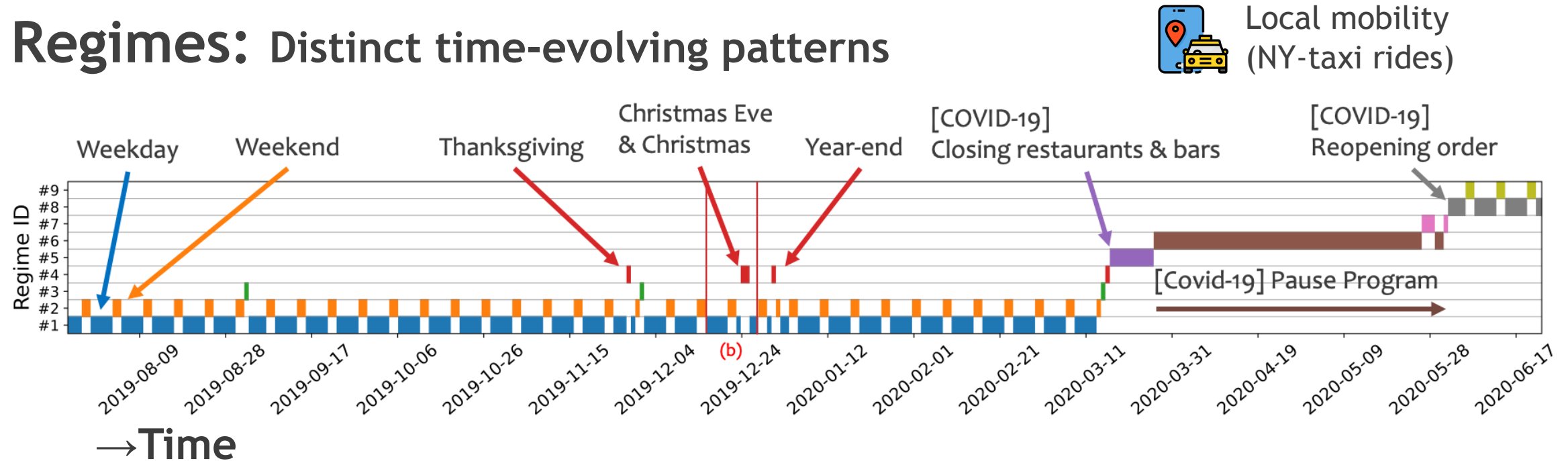
Our Questions

- Q. How can we **summarize** large, dynamic high-order tensor streams?
- Q. How can we see any hidden **patterns**, **rules**, and **anomalies**?

Our answer is ...
to focus on two types of patterns,
Regimes and **Components**

Our Answer: Regimes and Components

Regimes: Distinct time-evolving patterns



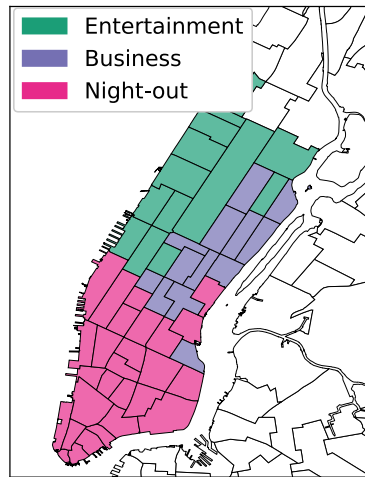
□ Summarize **semi-infinite** event stream into a handful number of segments

Our Answer: Regimes and Components

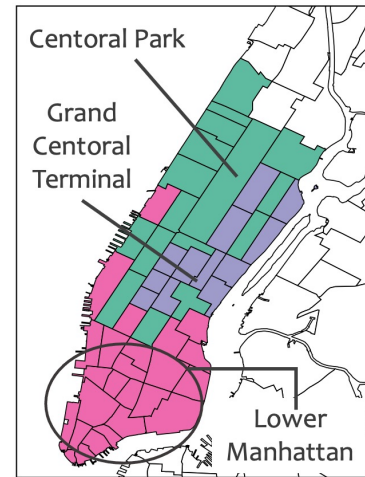
Components: Multi-aspect latent trends



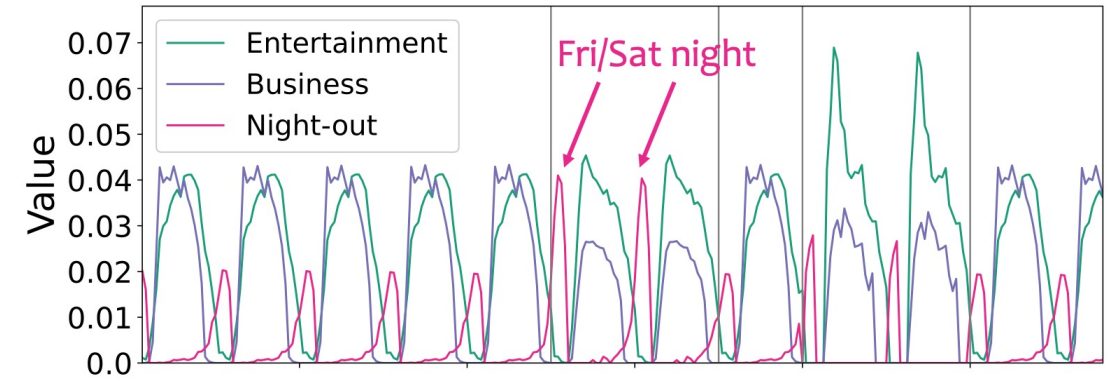
Local mobility
(NY-taxi rides)



Pick-up location



Drop-off location



Timestamp (Pick-up time)

□ Summarize **high-dimensional** and **sparse** events into major groups

Outline

Introduction

▶ **Model**

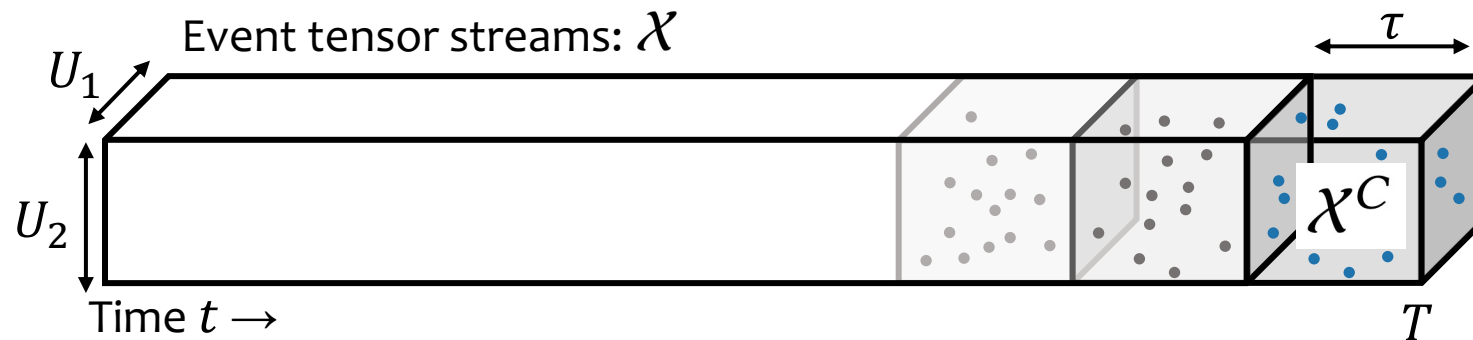
Algorithm

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Conclusion

Our Settings: Complex Time-stamped Event Streams

- Event stream, which consist of {M attributes + Timestamp}
→ **M+1th-order tensor stream** $\mathcal{X} \in \mathbb{N}^{U_1 \times \dots \times U_M \times T}$
- Continuously obtain **current tensors** $\mathcal{X}^C \in \mathbb{N}^{U_1 \times \dots \times U_M \times \tau}$



Proposed Model

Q1. What is the simplest mathematical model for **components**?

Q2. How can we represent **regimes** and summarize the whole stream?

Q3. How can we formulate **the summarization problem**?

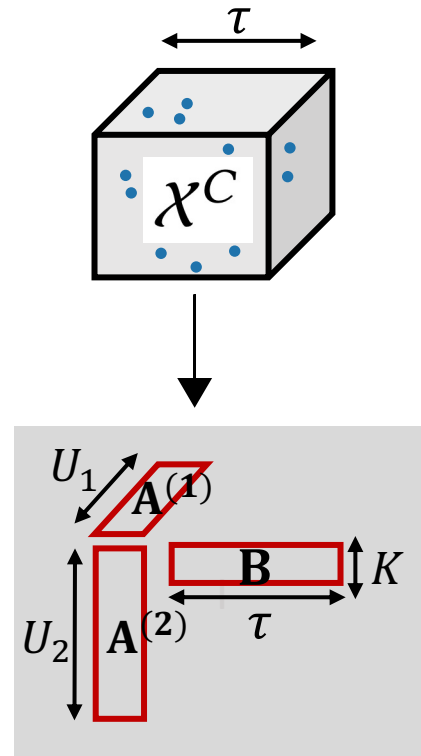
G1. Multi-aspect component factorization

G2. Compact description

G3. Problem formulation in a data compression paradigm

G1. Multi-aspect Component Factorization

Goal: to describe a high-dimensional and sparse tensor χ^C as compact and interpretable model



Component matrices

Multi-aspect Component factorization

- ❑ Model the generative process of events
- ❑ Assume that there are K major trends/**components**
- ❑ k -th **component** is defined by probability distribution w.r.t. M attributes and time

$$\mathbf{A}_k^{(m)} \in \mathbb{R}^{U_m}, \mathbf{B}_t \in \mathbb{R}^K$$

$$\mathbf{A}_k^{(m)} \sim \text{Dirichlet}(\alpha^{(m)}), \mathbf{B}_t \sim \text{Dirichlet}(\beta)$$

G1. Multi-aspect Component Factorization

The generative process:

- For each component $k = 1, \dots, K$:
 - For each attribute $m = 1, \dots, M$:
 - * $\mathbf{A}_k^{(m)} \sim \text{Dirichlet}(\sum_{l=1}^L \alpha^{(m)}_l \hat{\mathbf{A}}_k^{(m)})$
- For each time $t = 1, \dots, \tau$:
 - $\mathbf{B}_t \sim \text{Dirichlet}(\sum_{l=1}^L \beta_l \hat{\mathbf{B}}_t)$
 - For each entry $j = 1, \dots, N_t$:
 - * $z_{t,j} \sim \text{Multinomial}(\mathbf{B}_t)$ // Draw a latent component $z_{t,j}$
 - * For each attribute $m = 1, \dots, M$:
 - $e_{t,j}^{(m)} \sim \text{Multinomial}(\mathbf{A}_{z_{t,j}}^{(m)})$, // Draw a unit in each attribute

Capture temporal dependencies without storing tensors

Details in paper

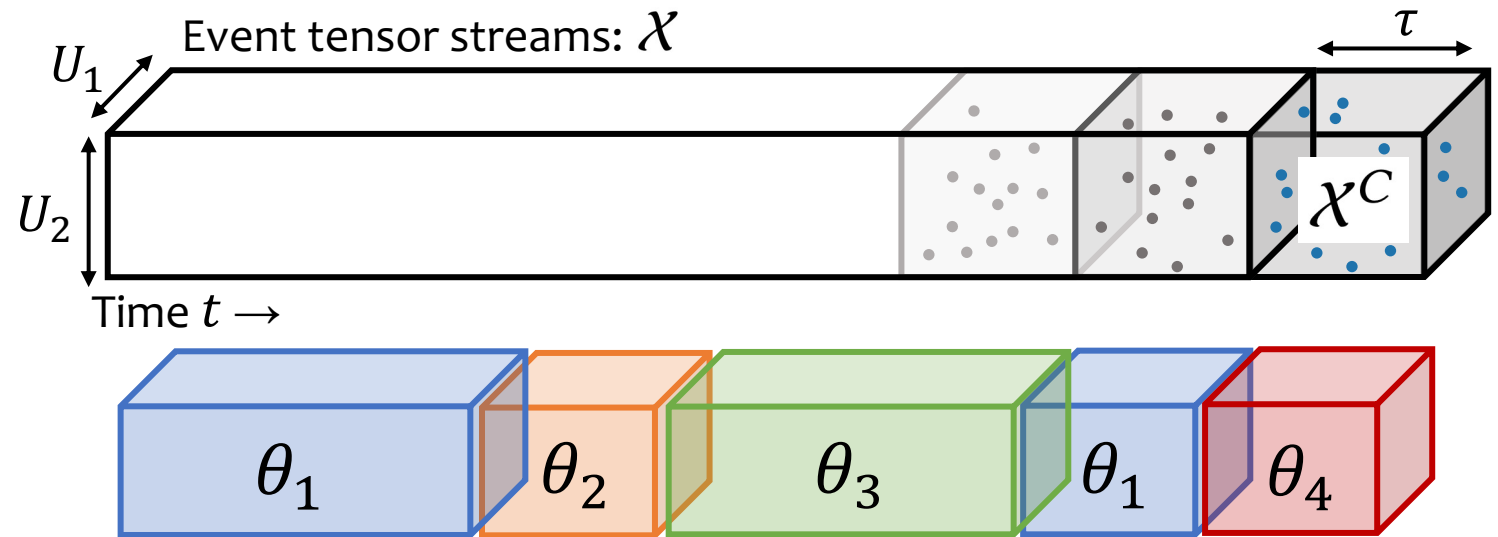
- ❑ **Summarize** sparse activity into K components
- ❑ **Mutli-aspect property:** handle arbitrary-order tensors
- ❑ **Online setting:** capture temporal dependencies without storing tensors

G2. Compact description

Goal: to represent the whole stream \mathcal{X} , containing distinct dynamical patterns

Regime:

$$\theta = \{ \{ \mathbf{A}^m \}_{m=1}^M, \mathbf{B} \}$$



Compact description: $\mathcal{C} = \{R, \Theta, G, \mathcal{S}\}$

- the number of regimes R and the regime set Θ
- the number of segments G and the assignments \mathcal{S}

G3. Problem Formulation: Data Compression Paradigm

What is good summarization?

- Minimum Description Length (MDL) principle:
“the more we can compress the data,
the more we can learn about their underlying patterns”
- Evaluate the total encoding cost,
which is used to losslessly compress the original data streams

Summarization Problem

Find the compact description \mathcal{C} , which minimizes the total encoding cost

$$\langle \mathcal{X}; \mathcal{C} \rangle = \underbrace{\langle \mathcal{C} \rangle}_{\text{Model coding cost}} + \underbrace{\langle \mathcal{X} | \mathcal{C} \rangle}_{\text{Data coding cost}}$$

G3. Problem Formulation: Data Compression Paradigm

- ❑ **Model Coding Cost:** the number of bits needed to describe the model \mathcal{C}
- ❑ **Data Coding Cost:** the coding cost of data \mathcal{X} given the model \mathcal{C}

Dimensionality Number of regimes Number of segments

$$\begin{aligned}
 \langle \mathcal{X}; \mathcal{C} \rangle &= \langle \mathcal{C} \rangle + \langle \mathcal{X} | \mathcal{C} \rangle \\
 &= \underbrace{\langle d \rangle}_{\text{Dimensionality}} + \underbrace{\langle R \rangle}_{\text{Number of regimes}} + \underbrace{\langle G \rangle}_{\text{Number of segments}} \\
 &\quad + \sum_{r=1}^R \underbrace{\langle \theta \rangle}_{\text{Each regime}} + \sum_{g=1}^G \underbrace{\langle s_g \rangle}_{\text{Each segment}} + \underbrace{\langle \mathcal{X} | \mathcal{C} \rangle}_{\text{Coding cost of each segment given regimes}}. \tag{6}
 \end{aligned}$$

$$\sum_{r=1}^R -\log P(\mathcal{X}[r] | \theta_r)$$

Details in paper

Outline

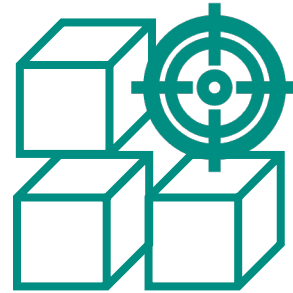
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▶ Algorithm

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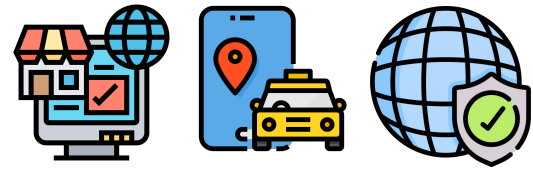


CubeScope

Streaming Algorithm: CubeScope

Given:

Complex time-stamped event streams



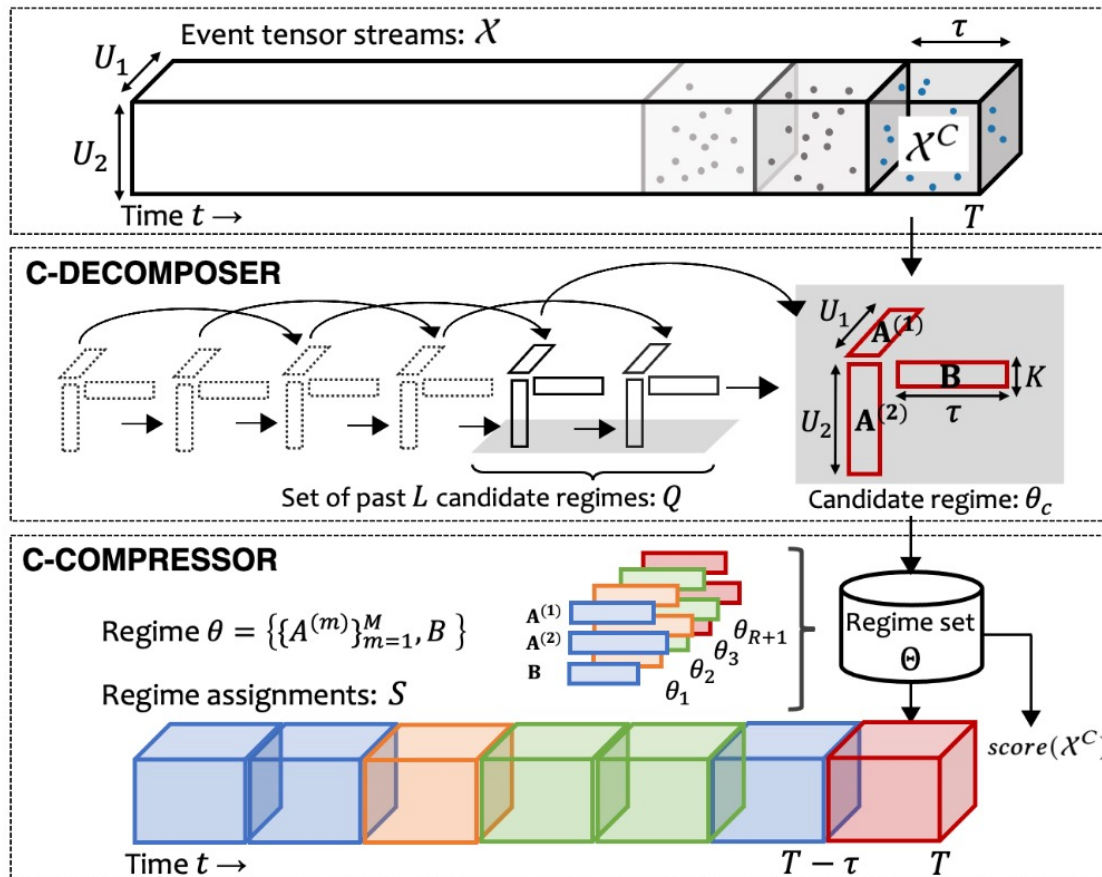
CubeScope

- Finds
 - Components (Multi-aspect latent trends/groups)
 - Regimes (Distinct time-evolving patterns)
- Detects anomalies and their types



Streaming Algorithm: CubeScope

Our **CubeScope** consists of two sub-algorithms:



□ C-Decomposer:

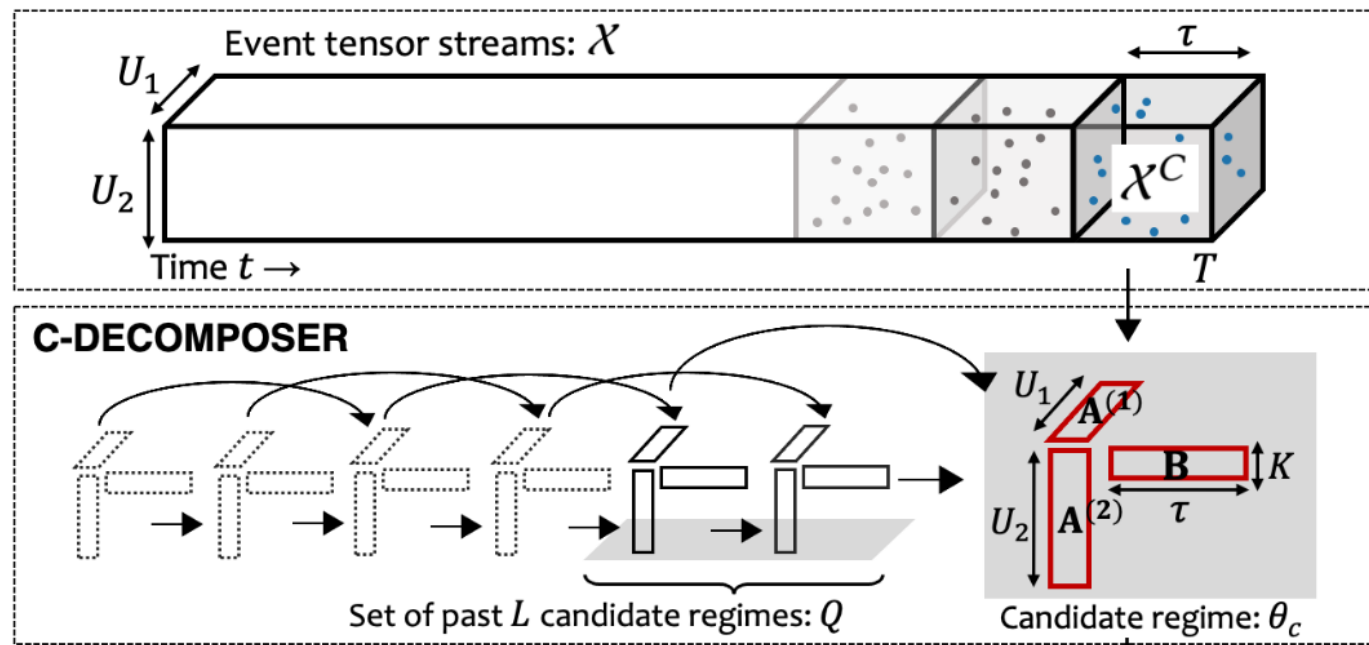
- incrementally monitors \mathcal{X}^C
- estimates a candidate regime θ_c

□ C-Compressor:

- Updates the compact description \mathcal{C}
- Measures the anomalousness of \mathcal{X}^C



C-Decomposer



□ Regime estimation with collapsed Gibbs sampling

$$p(z_{u_1, \dots, u_M, t} = k \mid \mathcal{X}^C, \mathbf{B}', \hat{\mathbf{B}}, \beta, \{\mathbf{A}^{(m)'} , \hat{\mathbf{A}}^{(m)}, \alpha^{(m)}\}_{m=1}^M)$$

$$\propto \frac{b'_{t,k} + \sum_{l=1}^L \beta_l \hat{b}_{t,k}}{\sum_{k=1}^K b'_{t,k} + L\beta} \cdot \prod_{m=1}^M \frac{a_{u_m,k}^{(m)'} + \sum_{l=1}^L \alpha^{(m)} l \hat{a}_{u_m,k}^{(m)}}{\sum_{u=1}^{U_m} a_{u,k}^{(m)'} + L\alpha^{(m)}}$$

$$\tilde{a}_{u,k}^{(m)} \propto \frac{a_{u,k}^{(m)} + \sum_{l=1}^L \alpha^{(m)} l \hat{a}_{u,k}^{(m)}}{\sum_{u=1}^{U_m} a_{u,k}^{(m)} + L\alpha^{(m)}}, \tilde{b}_{t,k} \propto \frac{b_{t,k} + \sum_{l=1}^L \beta_l \hat{b}_{t,k}}{\sum_{k=1}^K b_{t,k} + L\beta}$$

C-Decomposer is Efficient

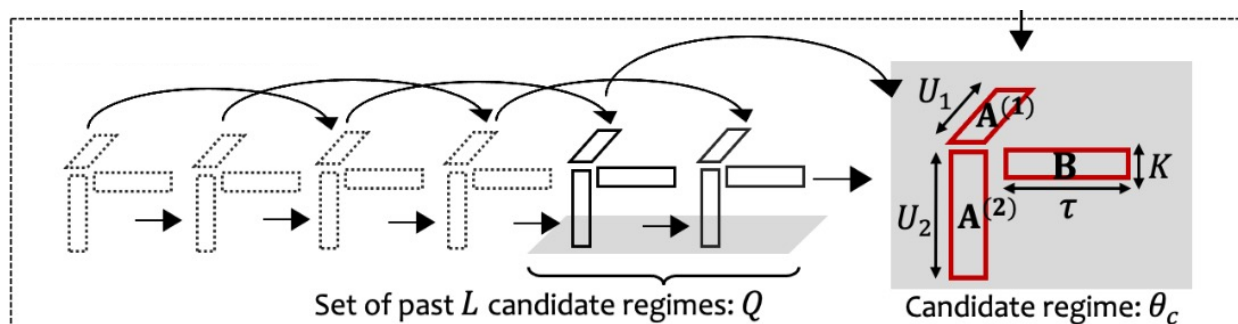
- Independent on dimensionality, i.e., it takes $O(N)$, N: the number of events
- Conventional algorithms (e.g., ALS) are expensive for high-order tensor these scale w.r.t. all the attributes, i.e., take $O(\prod_{m=1}^M U_m)$



C-Compressor

□ Insertion-based algorithm:

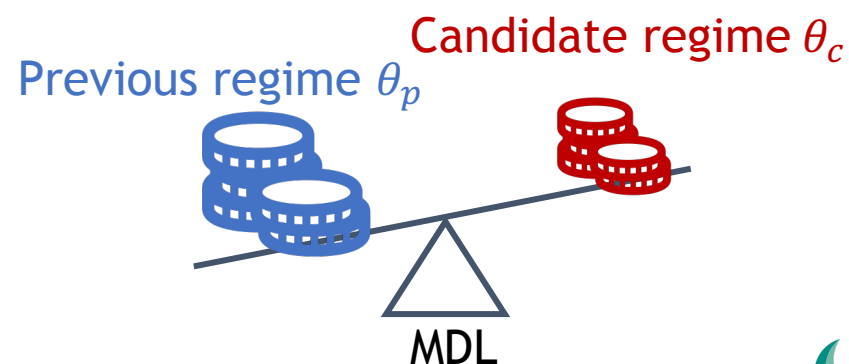
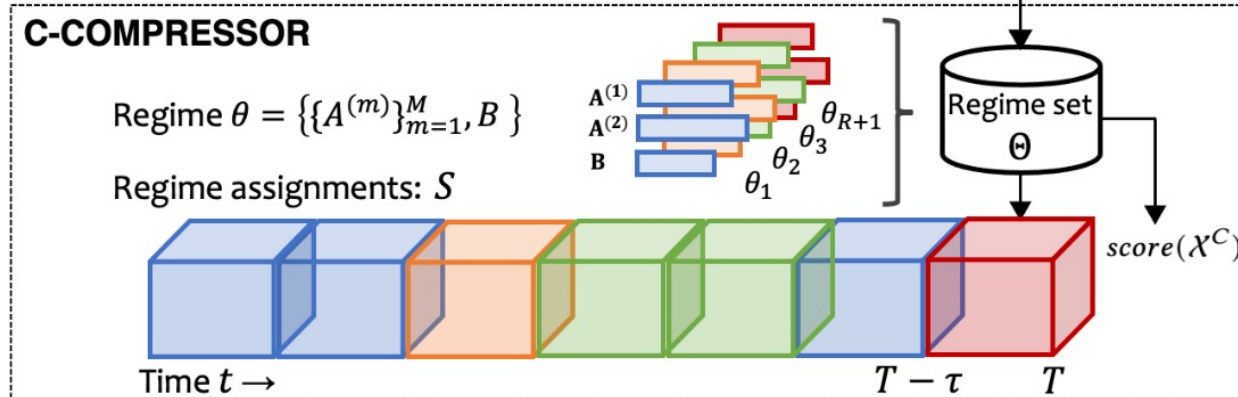
Maintains a reasonable description \mathcal{C} for \mathcal{X} and generates new regime if necessary



□ Compares encoding costs $\langle \mathcal{X}^C; \theta_* \rangle$ between θ_c and θ_p

$$\langle \mathcal{X}^C; \theta_* \rangle = \Delta \langle C \rangle + \langle \mathcal{X}^C | \theta_* \rangle, \quad (9)$$

$$\Delta \langle C \rangle = \log^*(R+1) - \log^*(R) + \langle \theta_* \rangle + \log^*(G+1) - \log^*(G) + \langle s \rangle, \quad (10)$$





C-Compressor: Stream Anomaly Detection

□ Compression-based anomaly detection

- Higher compression cost → higher anomalousness score

$$norm = \arg \max_{r \in R} |\mathcal{S}_r^{-1}|,$$

$$score(\mathcal{X}^C) = \langle \mathcal{X}^C | \theta_{norm} \rangle,$$

C-Compressor is Adaptive

- The concept of **normal changes** over time
→ Adaptively change the baseline to judge incoming tensors
- Data streams **contain multiple anomalies** over time
→ Discard anomalies from the baseline

Outline

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Algorithm

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Experimental Questions

We aim to evaluate that *CubeScope* has ...

Q1. Effectiveness:

How successfully does it discover meaningful patterns?

Q2. Accuracy:




How accurately does it achieve modeling, clustering, and anomaly detection?

Q3. Scalability:

How does it scale in terms of computational time?

Experimental Setup

12 datasets (8 real-world datasets + 4 synthetics)

Dataset	The form of entry	Order
Local Mobility: Ride information attributes & timestamp → #rides		
 #1 NYC-Taxi [8]	(Pick-up/Drop-off location ID, Time)	3
#2 Bike-Share [2]	(User's age, Start/End station ID, Time)	4
E-commerce: Purchase information attributes & timestamp → #purchases		
 #3 Jewelry [4]	(Price, Brand, Gem, Accessory type, Time)	4
#4 Electronics [3]	(Brand, Item category, Time)	3
Network traffic/intrusion: Access detail attributes & timestamp → #accesses		
 #5 AirForce [5]	(Protocol type, Service, Flag, Land, Duration Src/Dst bytes, Wrong fragment, Urgent, Time)	10
#6 External [1]	(Proto, Src/Dst IP Addr, Src/Dst Pt, Flags, Duration, Packets, Bytes, Time)	10
#7 OpenStack [1]	"	10
#8 Kyoto [9]	(Src/Dst bytes, Count, Same srv/Error/Srv error rate, Dst host error rate/same src port rate/srv errors rate, Dst host count/srv count, Duration, Service, Flag, Time)	15

12 Baselines

- LDA
- NTM
- TriMine
- K-means
- TICC
- CubeMarker
- T-LSTM
- DBSTREAM
- LOF
- iForest
- RRCF
- MemStream

Probabilistic
generative models

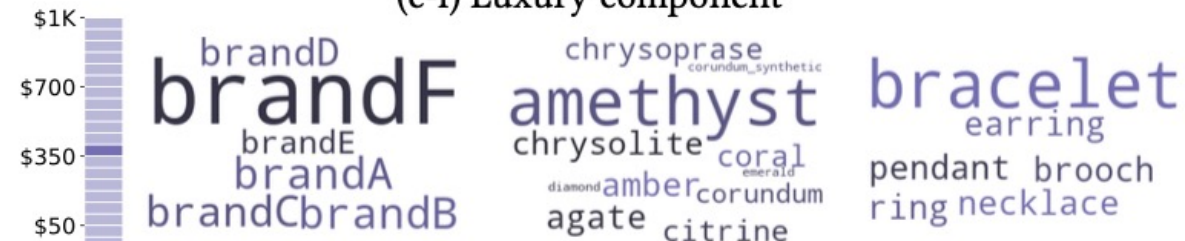
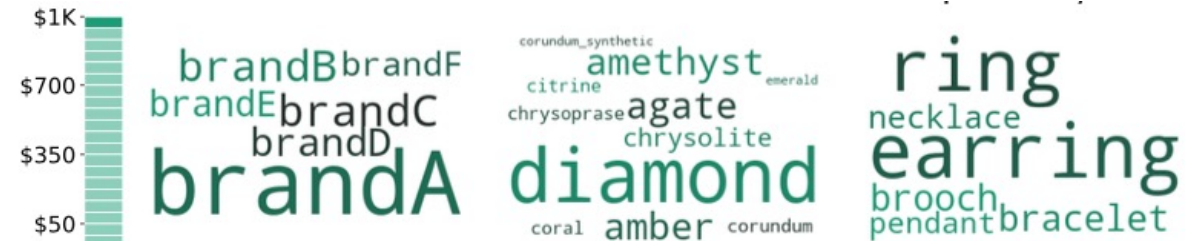
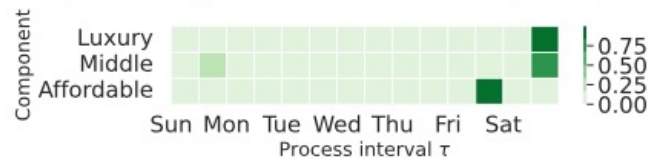
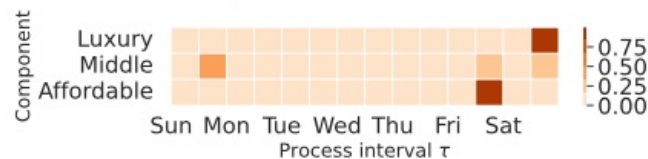
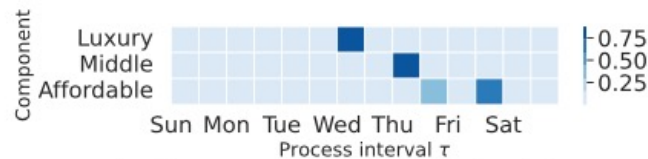
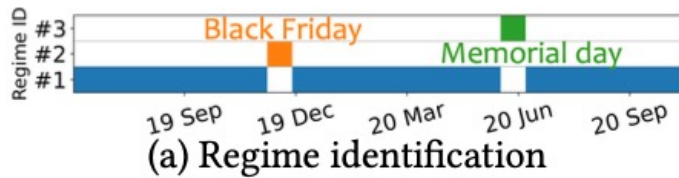
Clustering approaches
for time series, tensor,
and data streams

Unsupervised anomaly
detection methods



Q1. Effectiveness: Online Marketing Analytics

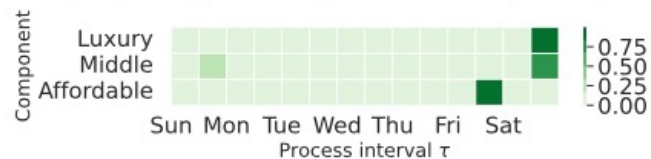
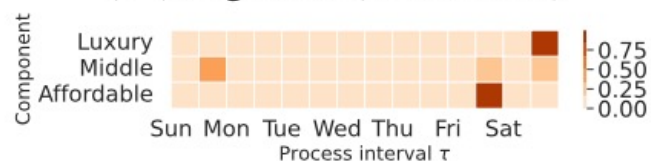
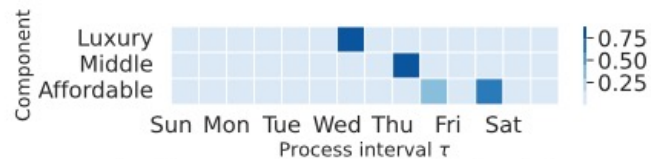
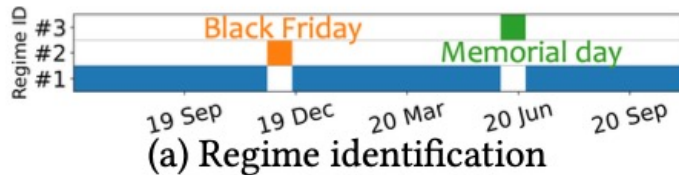
Jewelry Dataset: 4rd-order tensor stream
{Time, Price, Brand, Gem, Accessory type}





Q1. Effectiveness:

Jewelry Dataset: 4rd-order
 $\{Time, Price, Brand, Gem, \dots\}$



Regimes:

Distinct dynamical patterns

Changes in Purchase behavior



Online Marketing Analytics

tensor stream
Accessory type}



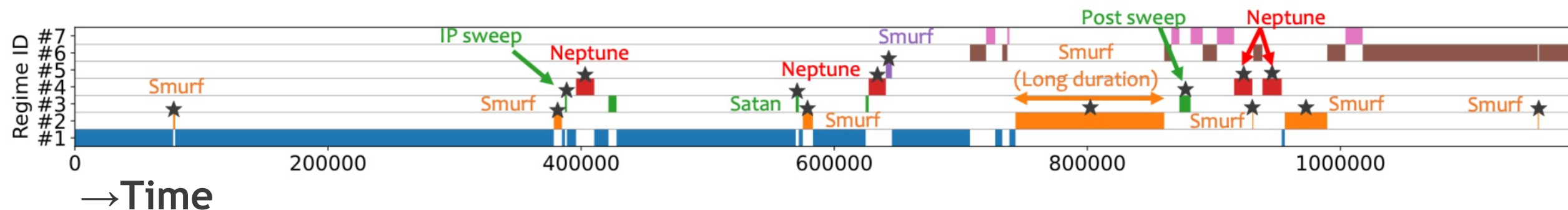
Components:
multi-aspect latent trends
User preferences



Q1. Effectiveness: Cybersecurity

AirForce Dataset: 10th-order tensor stream

{Time, Protocol type, Service, Flag, Land, Duration, Src/Dst bytes, Wrong fragment, Urgent}



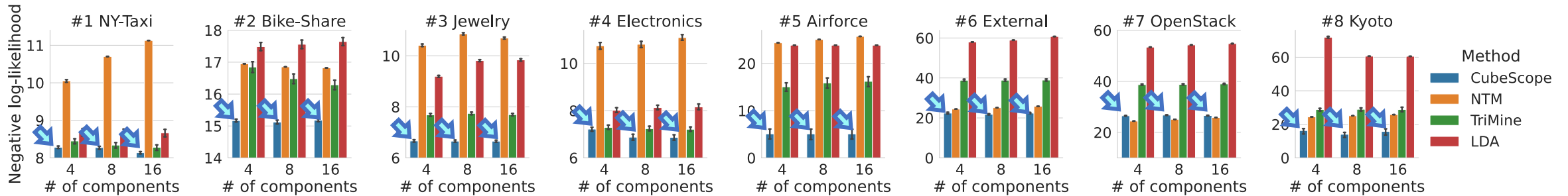
found **Regimes** that most corresponded to actual intrusions

- These intrusions arise over time and thus their **numbers**, **durations**, and **features** are unknown in advance

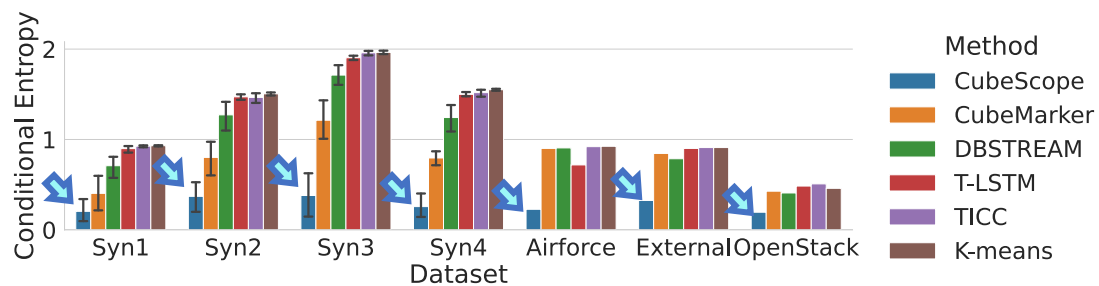
Q2. Accuracy: Modeling, Clustering, Anomaly Detection

“How does *CubeScope* achieve modeling, clustering, and anomaly detection?”

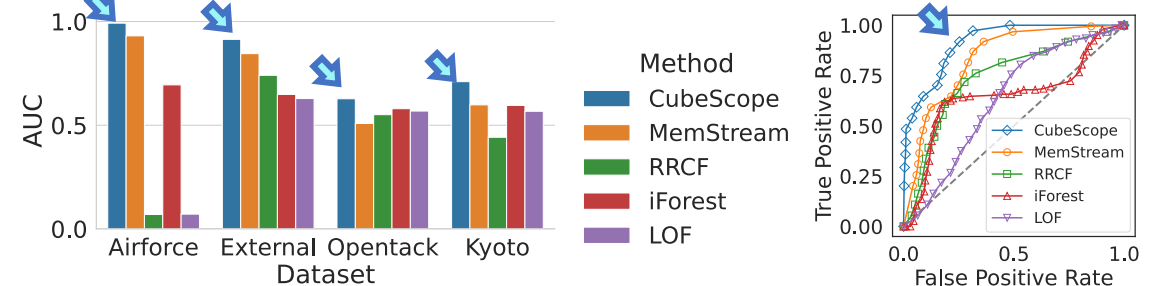
[Modeling] Negative log-likelihood: lower is better



[Clustering] CE score: lower is better



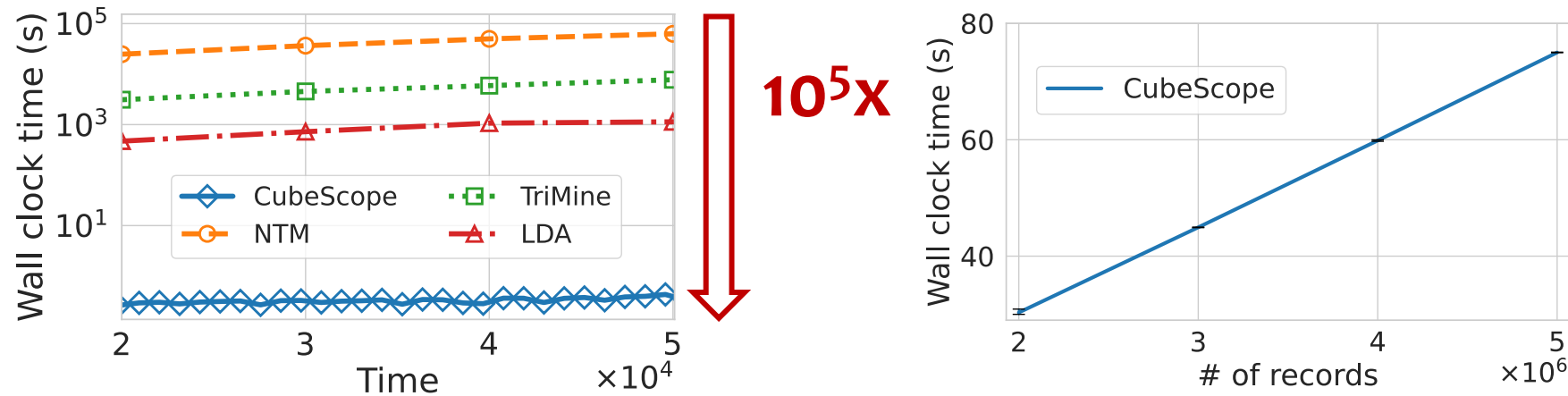
[Anomaly Detection] AUC score: higher is better



CubeScope consistently outperforms its baselines

Q3. Scalability

“How does *CubeScope* scale in terms of *computational time*?”



CubeScope is **up to 312,000x faster** than baselines and **scales linearly**

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Conclusion

Effective

- ❑ Introduce **regimes** and **components**
- ❑ Formulate **the summarization problem** for capturing these patterns
- ❑ Design **CubeScope** to solve the summarization problem

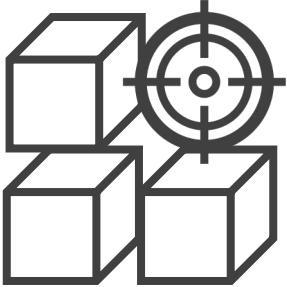
General

- ❑ Perform **data compression**, **pattern discovery**, and **anomaly detection**
- ❑ Practical in **multiple domains**,
such as local mobility, online market analytics, and cybersecurity

Scalable

- ❑ Fast and **constant computational time**
w.r.t. the entire stream length and its dimensionality

Thank you!



CubeScope

Data&Code:

